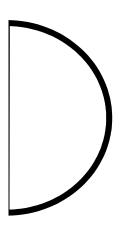


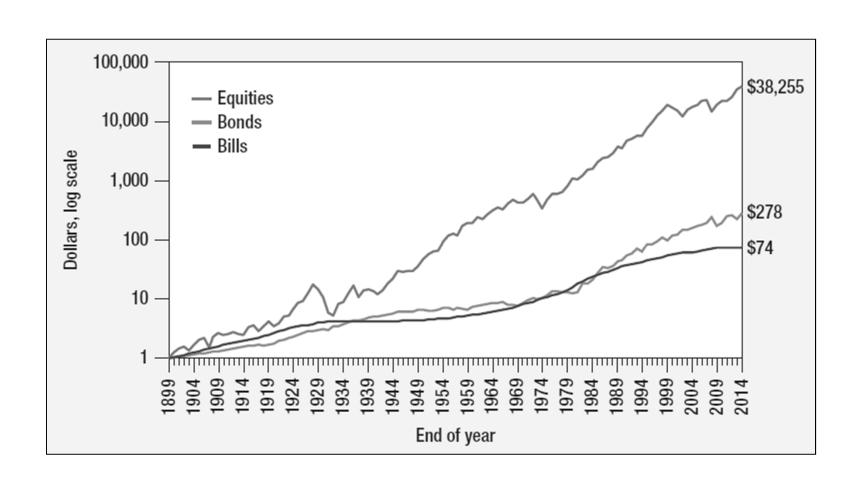
INTRODUCTION TO RISK AND RETURN



Topics Covered

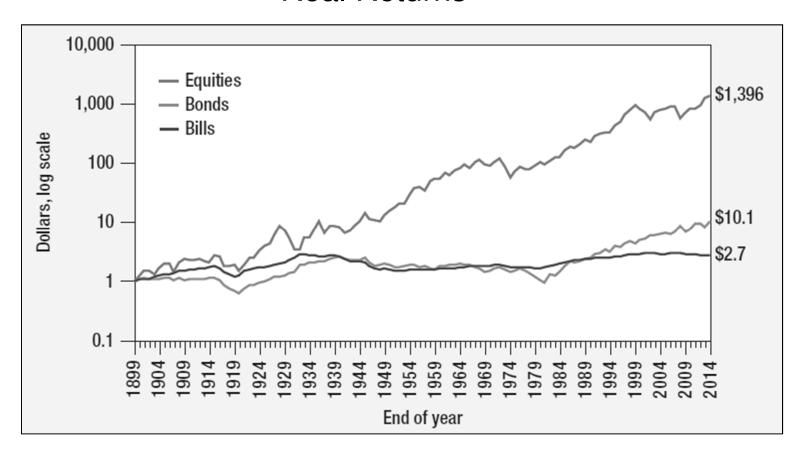
- Over a Century of Capital Market History in One Easy Lesson
- Measuring Portfolio Risk
- Calculating Portfolio Risk
- How Individual Securities Affect Portfolio Risk
- Diversification & Value Additivity

The Value of an Investment of \$1 in 1899

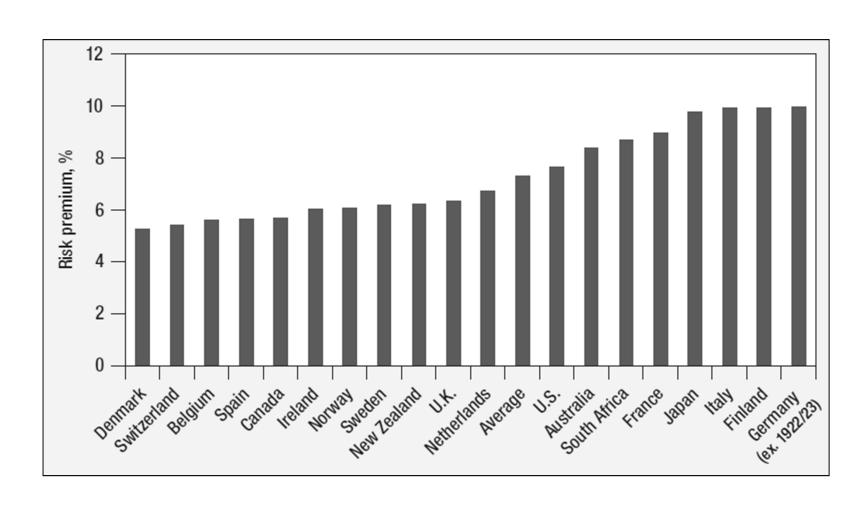


The Value of an Investment of \$1 in 1899

Real Returns

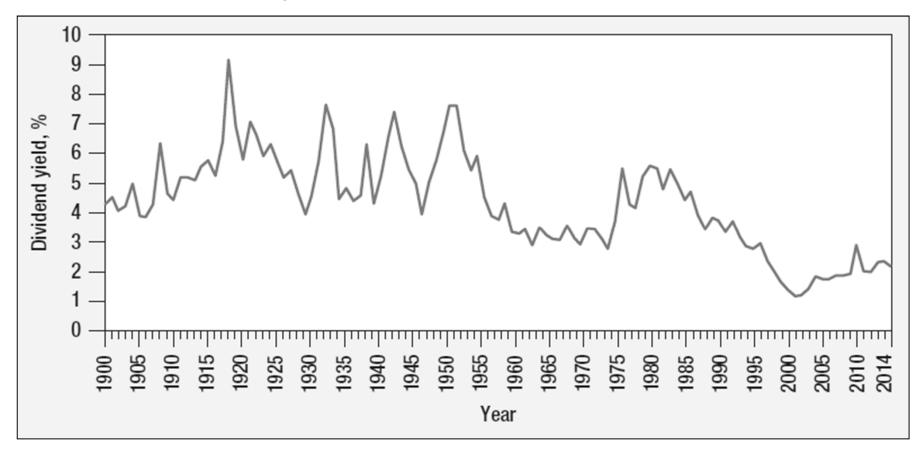


Average Market Risk Premiums (by country)



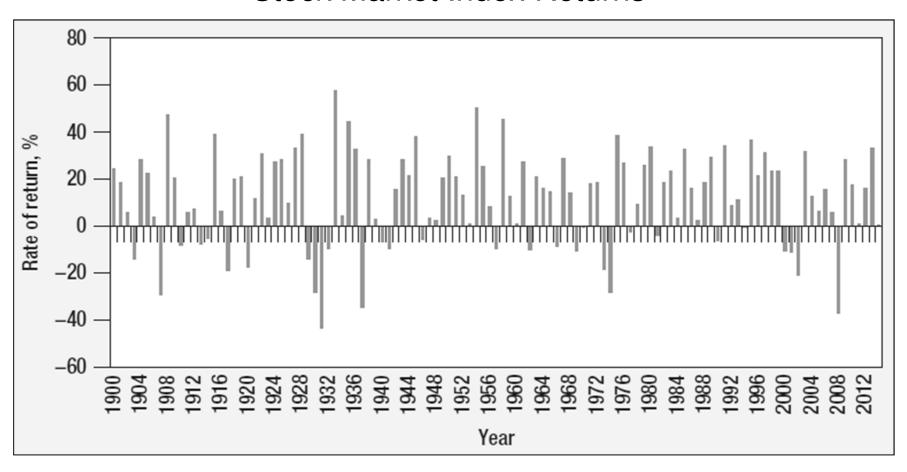
Dividend Yield

Dividend yields in the U.S. 1900–2014



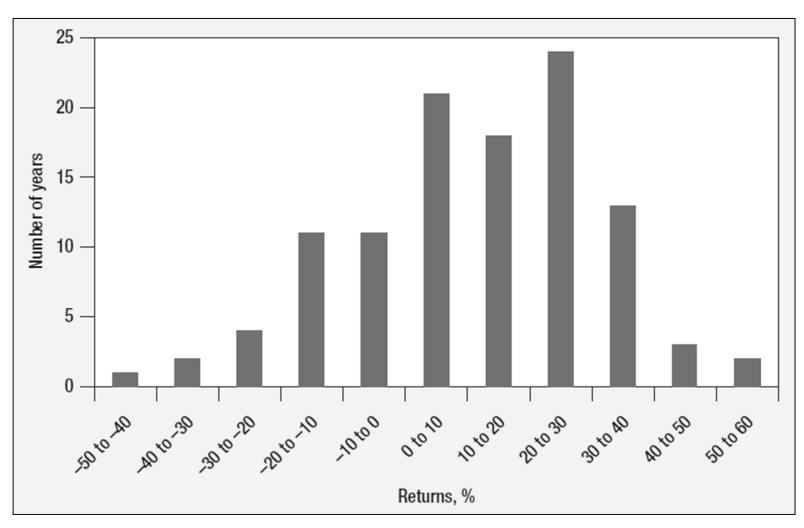
Rates of Return 1900-2011

Stock Market Index Returns



Source: E. Dimson, P. R. Marsh, and M. Staunton, *Triumph of the Optimists: 101 Years of Investment Returns* (Princeton, NJ: Princeton University Press, 2002), with updates provided by the authors.

Histogram of Annual Stock Market Returns (1900-2014)



Variance

- Average value of squared deviations from mean
- A measure of volatility

Standard Deviation

- Average value of squared deviations from mean
- A measure of volatility

Coin Toss Game-calculating variance and standard deviation

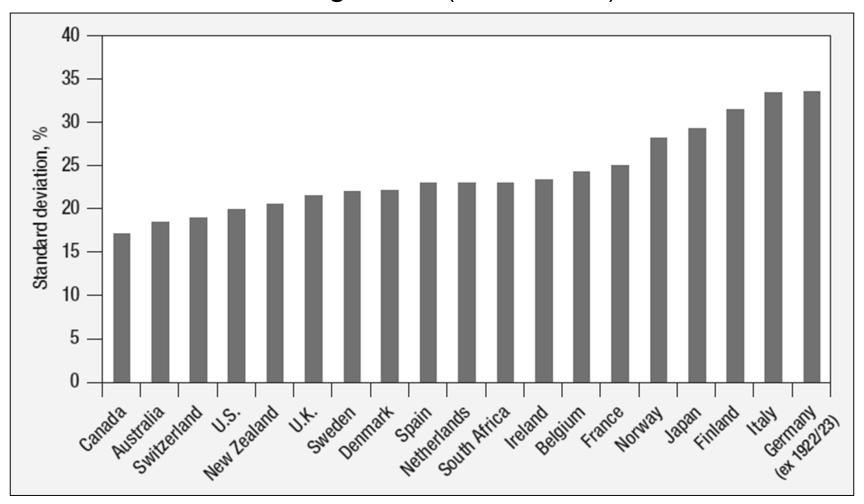
(1) Percent Rate of Return (\tilde{r})	(2) Deviation from Expected Return ($\tilde{r}-r$)	(3) Squared Deviation $(\tilde{r} - r)^2$	(4) Probability	(5) Probability × Squared Deviation	
+40	+30	900	0.25	225	
+10	0	0	0.5	0	
-20	-30	900	0.25	225	
Variance = expected value of $(\tilde{r} - r)^2 = 450$					
Standard deviation = $\sqrt{\text{variance}} = \sqrt{450} = 21$					

Portfolio rate of return
$$=$$
 $\left(\begin{array}{c} \text{fraction of portfolio} \\ \text{in first asset} \end{array}\right) \times \left(\begin{array}{c} \text{rate of return} \\ \text{on first asset} \end{array}\right)$ $+$ $\left(\begin{array}{c} \text{fraction of portfolio} \\ \text{in second asset} \end{array}\right) \times \left(\begin{array}{c} \text{rate of return} \\ \text{on second asset} \end{array}\right)$

Equity Market Risk (by country)

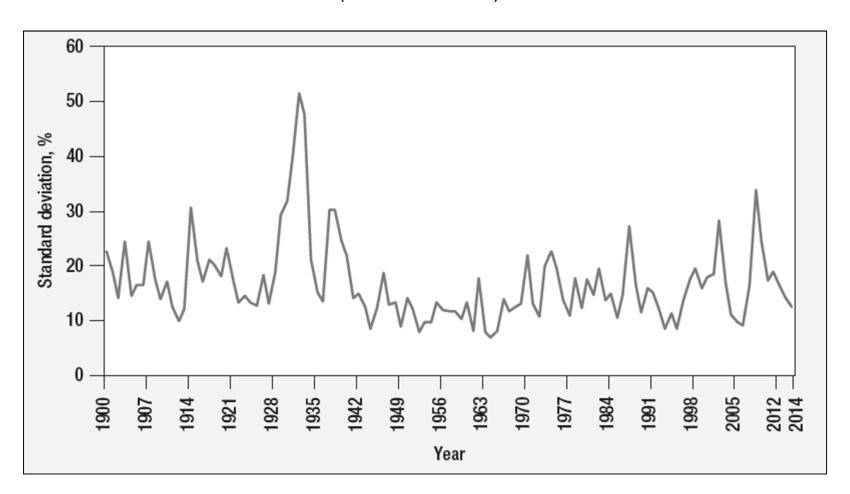
7-12

Average Risk (1900-2014)



7-13

Annualised Standard Deviation of the DJIA over the preceding 52 weeks (1900 – 2014)



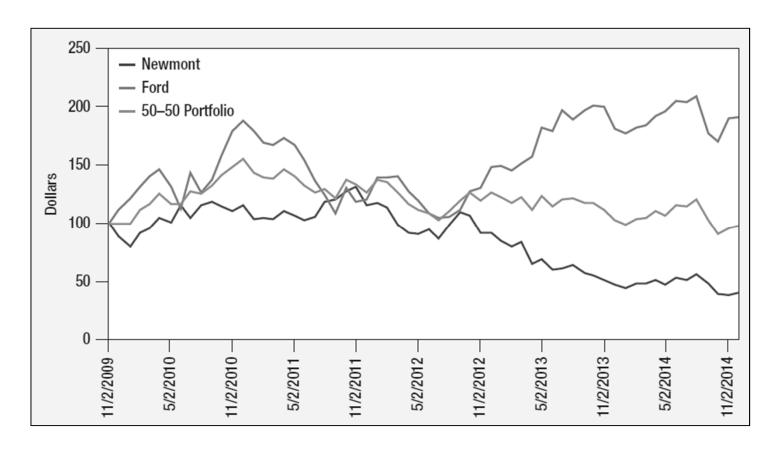
<u>Diversification</u> - Strategy designed to reduce risk by spreading the portfolio across many investments.

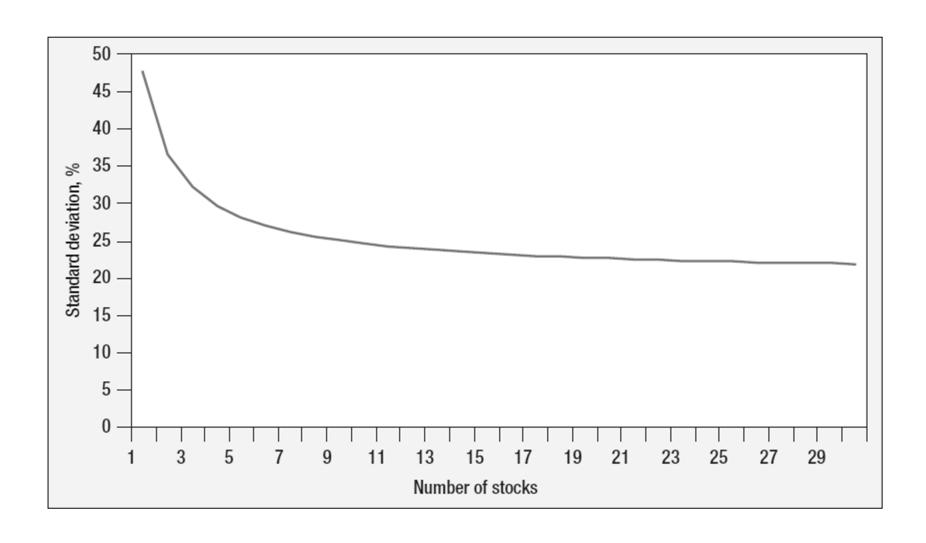
<u>Unique Risk</u> - Risk factors affecting only that firm. Also called "diversifiable risk."

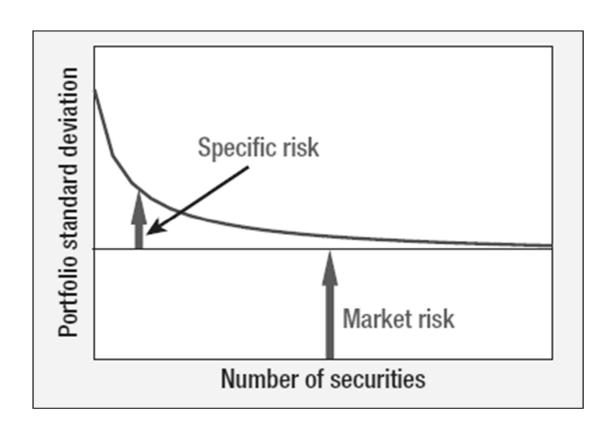
Market Risk - Economy-wide sources of risk that affect the overall stock market. Also called "systematic risk."

Comparing Returns

The value of a portfolio evenly divided between Newmont Mining and Ford was less volatile than either stock on its own. The assumed initial investment is \$100.







The variance of a two stock portfolio is the sum of these four boxes

	Stock 1	Stock 2
Stock 1	$X_1^2\sigma_1^2$	$x_1 x_2 \sigma_{12} =$
	101	$x_1x_2\rho_{12}\sigma_1\sigma_2$
Stock 2	$x_1x_2\sigma_{12} =$	$x_2^2\sigma_2^2$
Stoon 2	$x_1x_2\rho_{12}\sigma_1\sigma_2$	

Example

Suppose you invest 60% of your portfolio in JNJ and 40% in Ford. The expected dollar return on your JNJ is 8.0% and on Ford is 18.8%. The expected return on your portfolio is:

Expected return =
$$(.60 \times 8.0) + (.40 \times 18.8) = 12.3\%$$

Example

Suppose you invest 60% of your portfolio in JNJ and 40% in Ford. The expected dollar return on your JNJ is 8.0% and on Ford is 18.8%. The standard deviation of their annualised daily returns are 13.2% and 31.0%, respectively. Assume a correlation coefficient of 1.0 and calculate the portfolio variance.

	JNJ	Ford	
JNJ	$x_1^2 \sigma_1^2 = (.60)^2 \times (13.2)^2$	$x_1 x_2 \rho_{12} \sigma_1 \sigma_2 = .40 \times .60$	
		×1×13.2×31.0	
Ford	$x_1 x_2 \rho_{12} \sigma_1 \sigma_2 = .40 \times .60$ $\times 1 \times 13.2 \times 31.0$	$x_2^2 \sigma_2^2 = (.40)^2 \times (31.0)^2$	
	$\times 1 \times 13.2 \times 31.0$	$X_2 O_2 = (.40) \times (31.0)$	

Example

Suppose you invest 60% of your portfolio in JNJ and 40% in Ford. The expected dollar return on your JNJ is 8.0% and on Ford is 18.8%. The standard deviation of their annualized daily returns are 13.2% and 31.0%, respectively. Assume a correlation coefficient of 1.0 and calculate the portfolio variance.

Portfolio variance=
$$[(.60)^2 \times (13.2)^2]$$

+ $[(.40)^2 \times (31.0)^2]$
+ $2(.40 \times .60 \times 1 \times 13.2 \times 31.0) = 412.90$

Standard deviation =
$$\sqrt{412.90}$$
 = 20.3%

Example

Suppose you invest 60% of your portfolio in JNJ and 40% in Ford. The expected dollar return on your JNJ is 8.0% and on Ford is 18.8%. The standard deviation of their annualized daily returns are 13.2% and 31.0%, respectively. Assume a correlation coefficient of .019 and calculate the portfolio variance.

Portfolio variance =
$$[(.60)^2 \times (13.2)^2]$$

+ $[(.40)^2 \times (31.0)^2]$
+ $2(.40 \times .60 \times 0.19 \times 13.2 \times 31.0) = 253.80$

Standard deviation =
$$\sqrt{253.80}$$
 = 15.90%

Another Example

Suppose you invest 60% of your portfolio in JNJ and 40% in Ford. The expected dollar return on your JNJ is 8.0% and on Ford is 18.8%. The standard deviation of their annualized daily returns are 13.2% and 31.0%, respectively. Assume a correlation coefficient of -1.00 and calculate the portfolio variance.

Portfolio variance =
$$[(.60)^2 \times (13.2)^2]$$

+ $[(.40)^2 \times (31.0)^2]$
+ $2(.40 \times .60 \times (-1.00) \times 13.2 \times 31.0) = 20.1$

Standard deviation =
$$\sqrt{20.10}$$
 = $\boxed{4.50\%}$

Expected portfolio return =
$$(x_1 r_1) + (x_2 r_2)$$

Portfolio variance =
$$x_1^2 \sigma_1^2 + x_2^2 \sigma_2^2 + 2(x_1 x_2 \rho_{12} \sigma_1 \sigma_2)$$

<u>Example</u>		Correlation Coefficient = .4		
Stocks	σ	% of Portfolio	Avg Return	
ABC Corp	28	60%	15%	
Big Corp	42	40%	21%	

Standard deviation = weighted avg = 33.6

Standard deviation = Portfolio = <u>28.1</u>

Real standard deviation:

=
$$(28^{2})(.6^{2}) + (42^{2})(.4^{2}) + 2(.4)(.6)(28)(42)(.4)$$

= 28.1 CORRECT

Return: r = (15%)(.60) + (21%)(.4) = 17.4%

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Portfolio Risk

<u>Example</u>		Correlation Coeffice	lation Coefficient = .4		
Stocks	σ	% of Portfolio	Avg Return		
ABC Corp	28	60%	15%		
Big Corp	42	40%	21%		

Standard deviation = weighted avg = 33.6

Standard deviation = portfolio = 28.1

Return = weighted avg = portfolio = 17.4%

Let's add New Corp. stock to the portfolio

<u>Example</u>		= .3	
Stocks	σ	% of Portfolio	Avg Return
Portfolio	28.1	50%	17.4%
New Corp	30	50%	19%

NEW standard deviation = weighted avg = 31.80

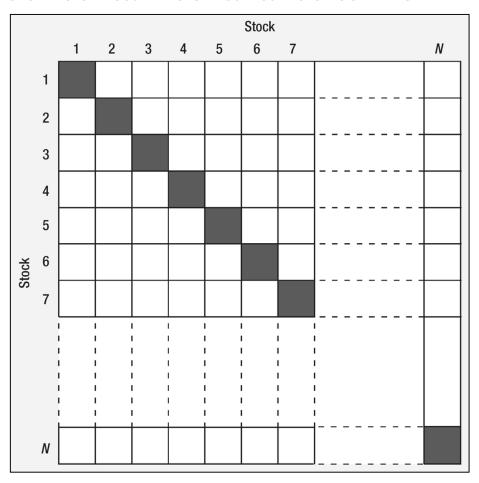
NEW standard deviation = portfolio = <u>23.43</u>

NEW return = weighted avg = portfolio = <u>18.20%</u>

NOTE: Higher return & Lower risk

How did we do that? <u>DIVERSIFICATION</u>

The shaded boxes contain variance terms; the remainder contain covariance terms.

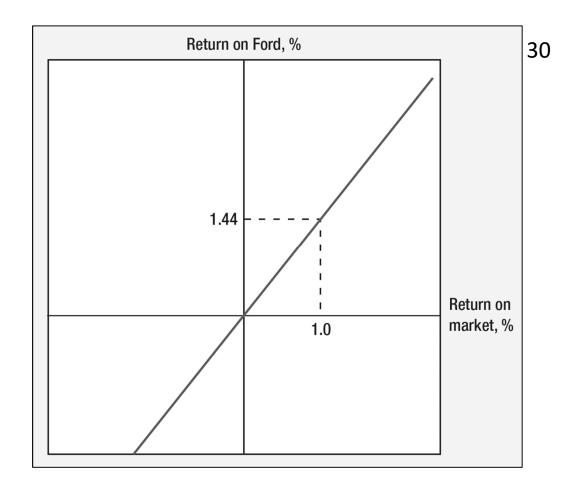


To calculate portfolio variance add up the boxes

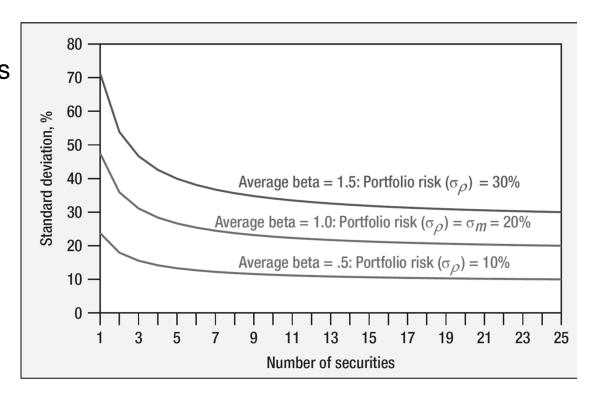
Market Portfolio - Portfolio of all assets in the economy. In practice a broad stock market index, such as the S&P Composite, is used to represent the market.

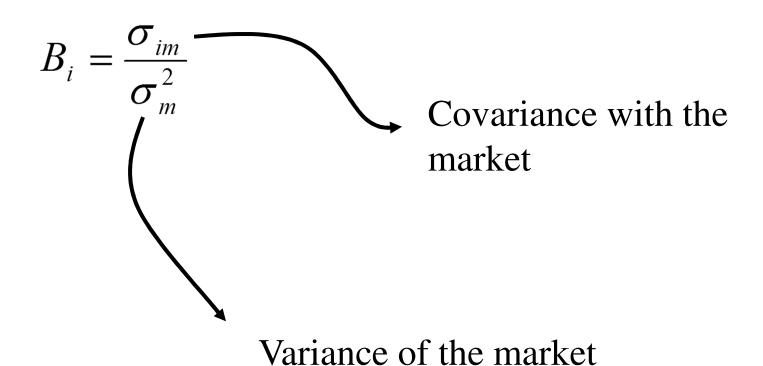
Beta - Sensitivity of a stock's return to the return on the market portfolio.

The return on Ford stock changes on average by 1.44% for each additional 1% change in the market return. Beta is therefore 1.44.



The green line shows that a well diversified portfolio of randomly selected stocks ends up with $\beta = 1$ and a standard deviation equal to the market's—in this case 20%. The upper red line shows that a well diversified portfolio with β = 1.5 has a standard deviation of about 30%—1.5 times that of the market. The lower blue line shows that a well-diversified portfolio with β = .5 has a standard deviation of about 10%—half that of the market.





Calculating the variance of the market returns and the covariance between the returns on the market and those of Anchovy Queen. Beta is the ratio of the variance to the covariance (i.e., $\beta = \sigma_{im}/\sigma_{m}^{2}$)

1	(1)	(2)	(3)	(4)	(5)	(6)	(7)
2							Product of
3				Deviation	Deviation	Squared	deviations
4				from	from average	deviation	from average
5		Market	Anchovy Q	average	Anchovy Q	from average	returns
6	Month	return	return	market return	return	market return	(cols 4×5)
7	1	- 8%	- 11%	– 10	– 13	100	130
8	2	4	8	2	6	4	12
9	3	12	19	10	17	100	170
10	4	- 6	– 13	- 8	– 15	64	120
11	5	2	3	0	1	0	0
12	6	8	6	6	4	36	24
13	Average	2	2		Total	304	456
14				Varian			
15				Covariance = σ_{im} = 456/6 = 76			
16				Beta (β)			