

From ML to ML: Two Disciplines, One Mission

– Making Sense of Imperfect Data

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SSC Gold Medal Address
Statistical Society of Canada Annual Meeting
June 2, 2026, Hamilton, Ontario, Canada

ML = Maximum Likelihood

ML = Machine Learning

(Statistics)

(AI)

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Two Disciplines, One Mission → Extracting Knowledge from Data



Part 1: A Brief Comparison of Statistical Science and Machine Learning

What Is Machine Learning?

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 - to improve performance, or
 - to make accurate predictions
- **Goodfellow, Bengio and Courville (2016)**:
Machine learning is **essentially a form of applied statistics** with
 - **increased emphasis** on using computers to estimate complicated functions, and
 - **decreased emphasis** on confidence intervals around these functions.

Over-Simplified Analogy: Learning to Cook

Statistical Science: Cooking with a Recipe



Machine Learning: Cooking without a Recipe



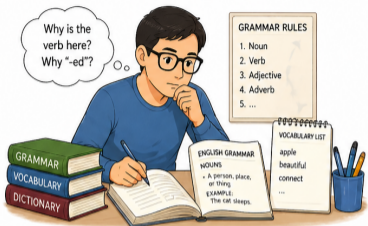
Create A New Dish:

guidance from recipes + experimentation



Over-Simplified Analogy: Acquiring One's Mother Tongue

Statistical Science: Adult Learning



- Structured learning: textbooks, grammar rules, vocabulary lists
- Study rules and grammar
- Focus on understanding "why"

Machine Learning: Infant Learning



- No formal grammar lessons
- Learn from patterns
- Improve with exposure



Patterns + Rules



Learn A New Language:
pattern-based + rule-based learning



**How do we learn from data
and generalize beyond it?**

Statistical Science

modeling + inference

uncertainty + interpretability

model → estimate → quantify uncertainty

Machine Learning

algorithms + optimization

prediction + scalability

represent → optimize → predict

Statistical Science

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Machine Learning

Primary Emphasis

inference and
uncertainty quantification

prediction and
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Data Structure

structured, curated
typically numerical

unstructured, digital
images, text, speech, graphs

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Parameter Dimension $p = O(10^N)$

small or moderate
 $N \approx 0-4$
e.g., regression

high or very high
 $N \approx 5-12$
e.g., neural networks

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Sample Size $n = O(10^N)$

small to moderate
 $N \approx 1-5$
e.g., clinical trials, surveys

large to massive
 $N \approx 5-15$
e.g., ImageNet, language

Statistical Science

Machine Learning

Statistical Science

Machine Learning

Framework & Scope

frequentist/Bayesian
parametric/semiparametric
/nonparametric models

supervised/unsupervised
/semi-supervised learning
reinforcement learning

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Machine Learning

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model/sample

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Identifiability

central requirement

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Interpretability	often high	often low

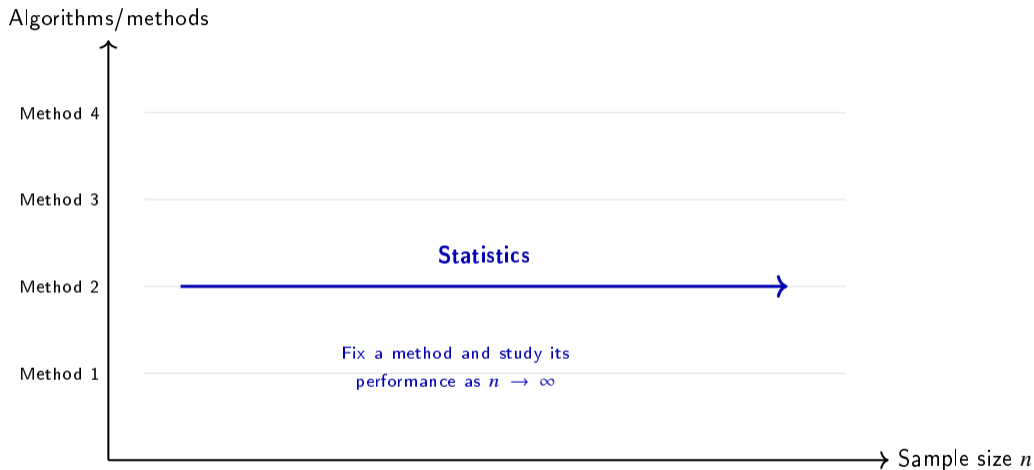
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Terminology	X : covariate/predictor Y : response/outcome	X : input/feature/instance Y : output/label

Validity Justification: Statistics vs Machine Learning



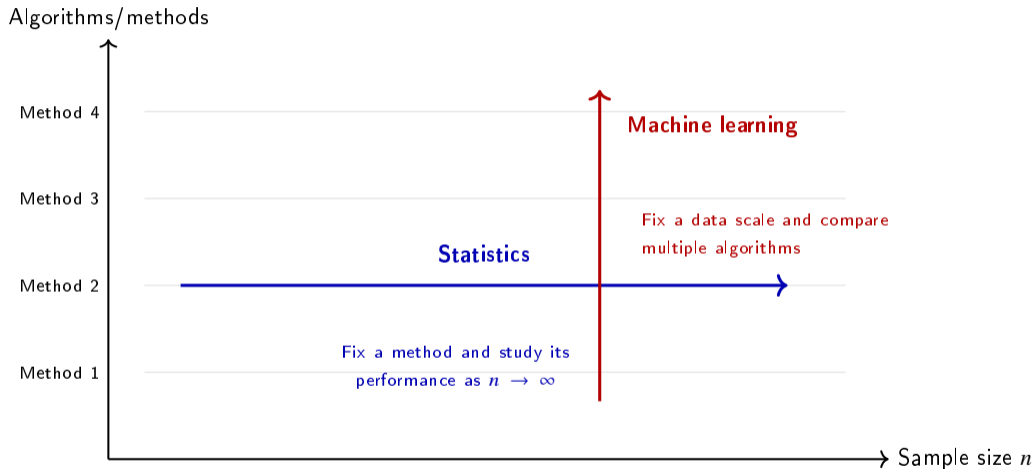
How do we justify that a method works?

Validity Justification: Statistics vs Machine Learning



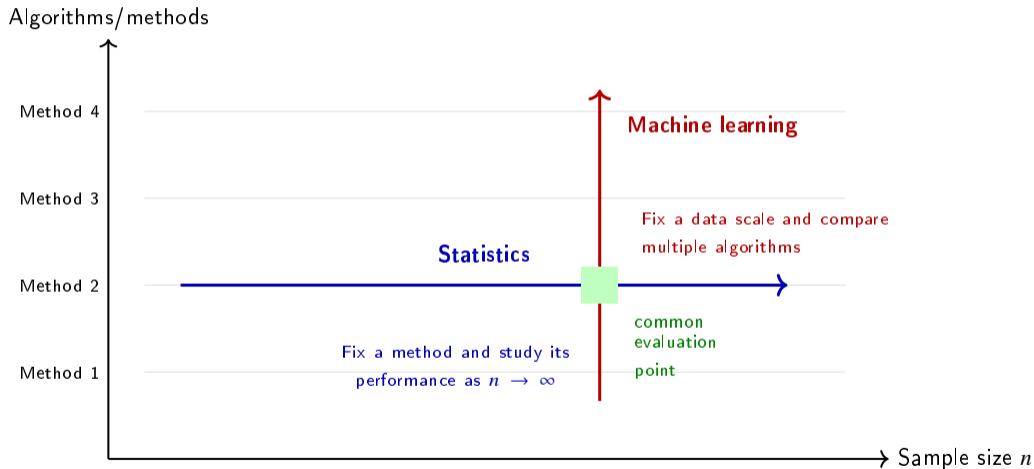
Statistics: often assess a method by considering the hypothetical scenario with $n \rightarrow \infty$

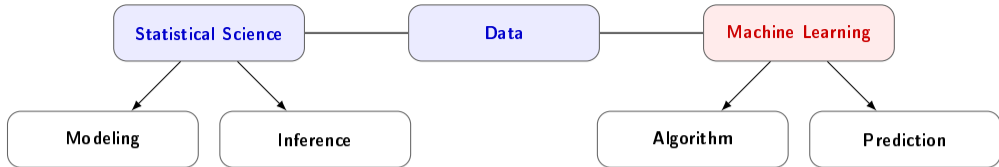
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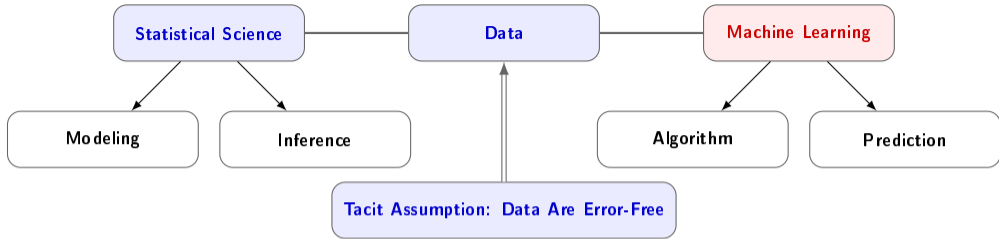


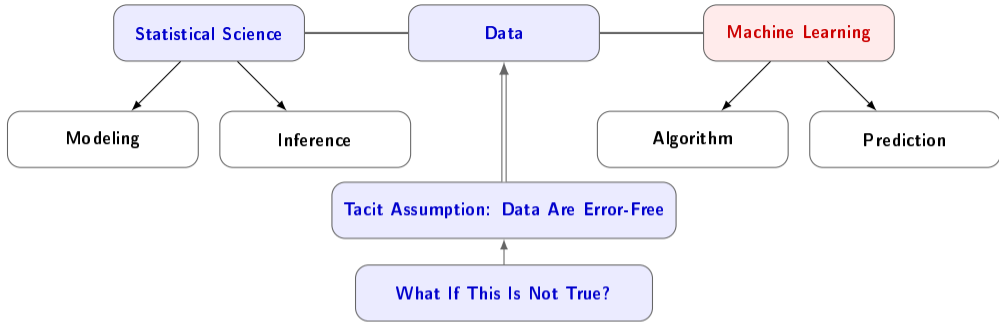
Machine Learning: often compare different methods/algorithms in a hypothetical class by fixing n

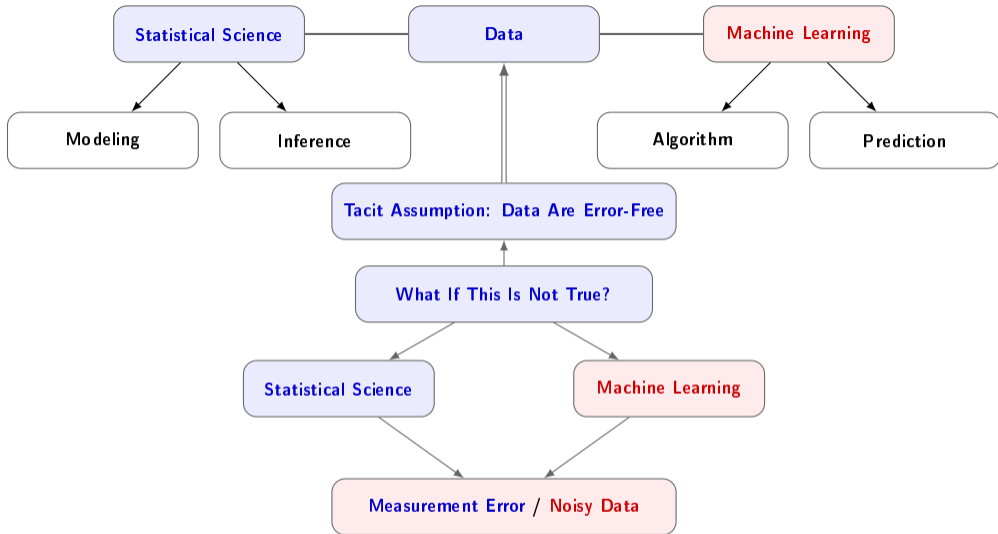
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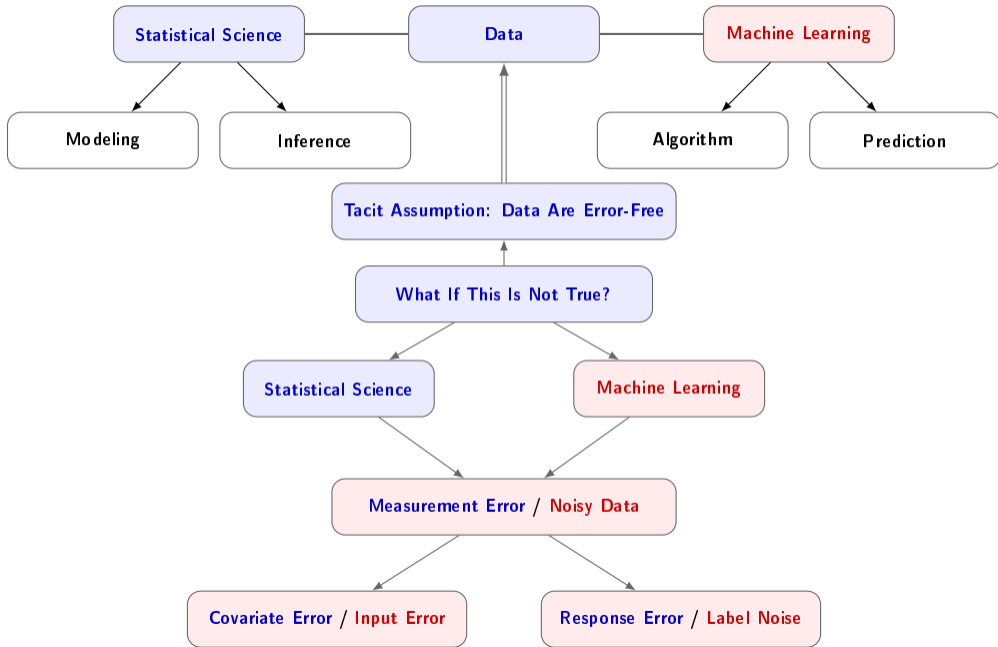












Part 2: Examples of Measurement Error and Noisy Data

Measurement Error in Statistical Analysis

Example: Reporting Error (Bollinger 1998)

- Reporting errors are typical in survey data. For example, it was found that
 - response error was negatively related to earnings
 - about 10% of the reporters grossly over-reported their income
 - There was greater measurement error among men than among women.
 - for men, a nonlinear relationship between reported earnings and true earnings existed, but for women the relationship was linear

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 - for men, a nonlinear relationship between reported earnings and true earnings existed, but for women the relationship was linear
- Remarks
 - Response error in income cannot be treated as additive white noise because of its relationship with gender and true earnings.
 - Measurement error is not related to age, education, and weeks worked.

Example of Blood Pressure (BP) – Long-Term Average Quantity

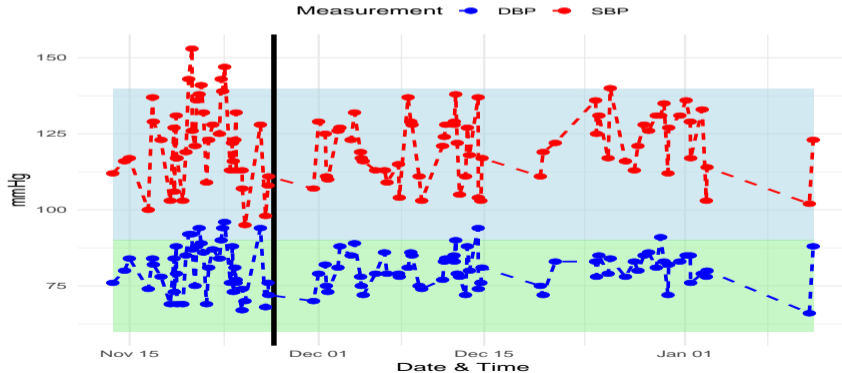
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Example: No Direct Measurement in Epidemiological Studies

- Some variables are difficult or even impossible to be measured directly.
- Common Examples:
 - body composition (total body fat or lean mass)
 - dietary intakes
 - physical activity
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Practical Procedure

- In the absence of direct measurements of some predictors, using surrogate measurements as a replacement seems to be a must.

Warning

- Addressing the induced error is important!

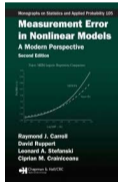


can we?

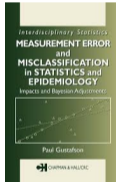
Data with
Measurement Error



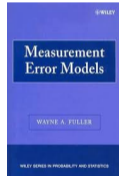
Useful
Conclusions



2006



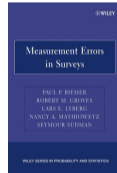
2004



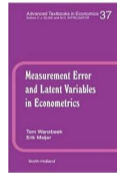
1987



2010



1991



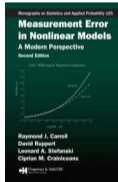
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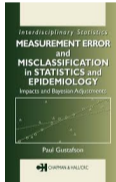
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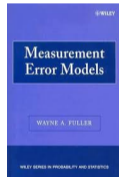
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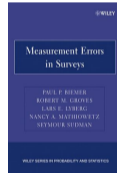
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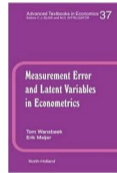
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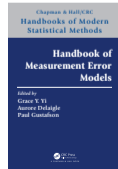
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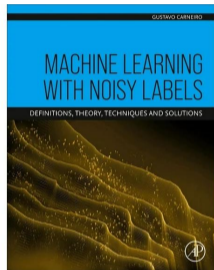


2017

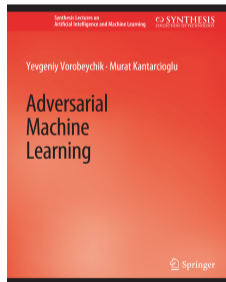


2021

Corrupted Data in Machine Learning











2024











2022

Image Recognition/Text Classification (Source: Carneiro 2024)

IMAGENET				
NOISY LABEL:	tick	patas monkey	dough	red panda
CLEAN LABEL:	yellow garden spider	gorilla	pizza	meerkat
CALTECH-256				
NOISY LABEL:	bear	llama	grapes	dolphin
CLEAN LABEL:	teddy bear	camel	mattress	kayak
IMDB	<p>David Morse and Andre Braugher are very talented actors, which is why I'm trying so hard to support this program. Unfortunately, an irrational plot, and very poor writing is making it difficult for me. I'm hoping that the show gets a serious overhaul, or that the actors find new projects that are worthy of them.</p>		<p>The ending made my heart jump up into my throat. I proceeded to leave the movie theater a little jittery. After all, it was nearly midnight. The movie was better than I expected. I don't know why it didn't last very long in the theaters or make as much money as anticipated. Definitely would recommend</p>	
NOISY LABEL:	positive		negative	
CLEAN LABEL:	negative		positive	

Dataset	Label Source	Cleanliness	Noise Source
ImageNet	human annotation via AMT + WordNet	high (in ILSVRC subset)	fine-grained confusion, human error
Caltech-256	manually grouped object categories	relatively clean	background clutter, overlapping categories
IMDB	derived from user rating scores	moderate	heuristic mismatch with sentiment, sarcasm, ambiguity

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Corrupted Labels

- The ratio of corrupted labels in real-world datasets was reported to range from **8.0% to 38.5%** (Song et al. 2023).
- Menze et al. (2014) reported average inter-reader variability of **74%–85%** for glioblastoma (a type of brain tumour) segmentation.

Part 3: How Do Statistical Methods and Machine Learning Techniques Interact?

(Some Illustrative Work)

Application 1: Noisy Label in Medical Imaging (Wang, Yi & Cao 2025)

- pneumoconiosis diagnosis from chest X-rays
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Data Feature

- 1,042 X-rays (NIOSH)
- 1–21 readers; scale 0–3

Label Noise

- Proxy ground truth via consensus
- Mislabeling: 21% (normal), 42% (abnormal)

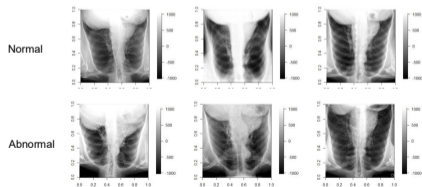


Figure 4: Chest image samples for normal individuals (top row) and abnormal individuals (bottom row).

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Our Method

ML + Statistics

- **ML**: afDNN learns representations
- **Statistics**: model annotator noise
- estimate true label distribution

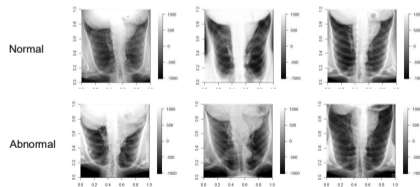


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- Automated methods:
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Key Issue

- No reliable ground truth labels

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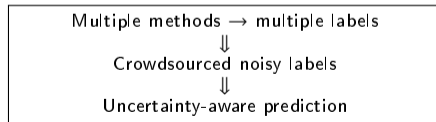
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Our Method

ML + Statistics

- **ML**: DNN architecture
- **Statistics**: treat algorithm-generated labels as crowdsourced annotations
- quantify uncertainty via conformal prediction



Supervised Learning/Classification

- In supervised learning, each data point is associated with a **label/annotation**

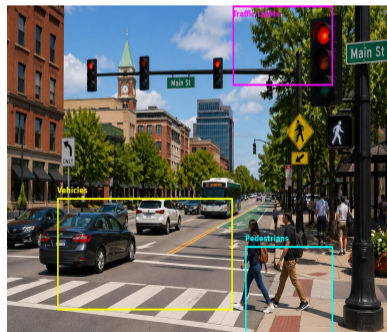
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Joint Work with Hui Guo and Boyu Wang
(NeurIPS, 2023)

Setup

$\mathcal{X} \subset \mathbb{R}^P$: feature space

$\mathcal{Y} = \{1, \dots, K\} \triangleq [K]$: label space

$\mathbf{x}_i \in \mathcal{X}$: input data

$y_i \in \mathcal{Y}$: **unobserved true label**

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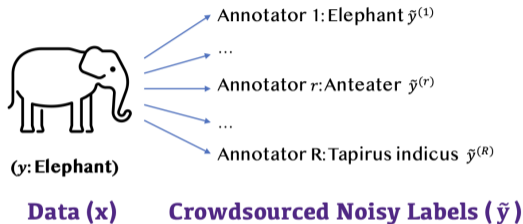
Crowdsourcing

each item is labeled by multiple annotators

$$\mathcal{D} = \{\mathbf{x}_i, \tilde{y}_i^{(1)}, \dots, \tilde{y}_i^{(R)}\}_{i=1}^N$$

R : #of annotators

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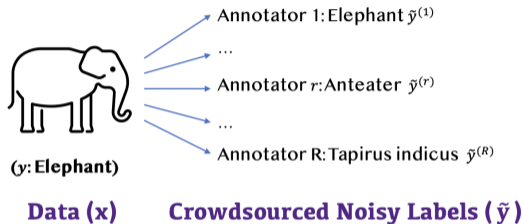
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Objective

use data with **noisy labels** to train a **classifier to correctly label new** input data

Assumption

R annotators **independently** label instances

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Noisy Label Probability

$$\begin{aligned}\mathbb{P}(\tilde{y}^{(1)}, \dots, \tilde{y}^{(R)} | \mathbf{x}) &= \prod_{r=1}^R \mathbb{P}(\tilde{y}^{(r)} | \mathbf{x}) \\ &= \prod_{r=1}^R \sum_{k \in \mathcal{Y}} \{ \mathbb{P}(\tilde{y}^{(r)} | y = k, \mathbf{x}) P(y = k | \mathbf{x}) \}\end{aligned}$$

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base model
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Remark

- Most available methods require the **instance independent** assumption:

$$\mathbb{P}(\tilde{y}^{(r)} | y = k, \mathbf{x}) = \mathbb{P}(\tilde{y}^{(r)} | y = k) \text{ for each } r$$

Proposed Modeling of Instance-Dependent Transition Matrices



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flexibly reflect two characteristics in the annotation process:

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Neural Networks

$$\tilde{y}^{(r)} \mid \{y = k, \mathbf{x}\} \sim G\{\mathbf{A}_0^{(r)} \psi_1(\mathbf{x}) + \mathbf{B}_0^{(k)} \psi_2(\mathbf{x})\}$$

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- influence of the **ground truth of class** (k)

Neural Networks

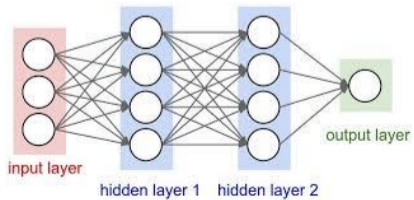
$$\tilde{y}^{(r)} \mid \{y = k, \mathbf{x}\} \sim G\{\mathbf{A}_0^{(r)} \psi_1(\mathbf{x}) + \mathbf{B}_0^{(k)} \psi_2(\mathbf{x})\}$$

where

$\mathbf{A}_0^{(r)}$ and $\mathbf{B}_0^{(k)}$: regression weights
 $\psi_1(\mathbf{x})$ and $\psi_2(\mathbf{x})$: unknown functions
 G : softmax function

Modeling $\psi_j(\mathbf{x})$ with Sparse Bayesian DNNs

With $j = 1, 2$,



Modeling $\psi_j(\mathbf{x})$ with Sparse Bayesian DNNs

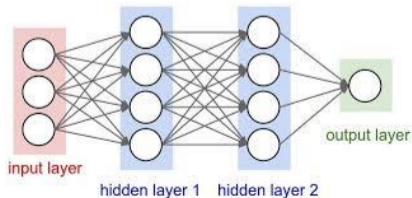
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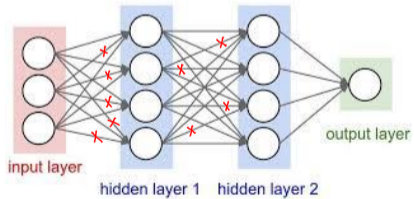
$$\psi_j(\mathbf{x}; \boldsymbol{\theta}^{(j)}) = \mathbf{W}^{(jH_j)} \sigma \left(\dots \sigma \left[\mathbf{W}^{(jh)} \sigma \left\{ \dots \sigma \left(\mathbf{W}^{(j1)} \mathbf{x} + \mathbf{b}^{(j1)} \right) \dots \right\} + \mathbf{b}^{(jh)} \right] \dots \right) + \mathbf{b}^{(jH_j)}$$

$\mathbf{W}^{(jh)}$: weight matrix for h th layer

$\mathbf{b}^{(jh)}$: bias for h th layer

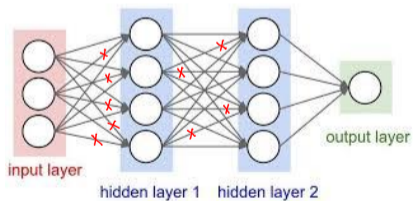
$\sigma(\cdot)$: activation function





Sparsity Indicator

$\gamma_l^{(j)} = I(\theta_l^{(j)} \neq 0)$ with associated parameter vector $\theta_l^{(j)}$

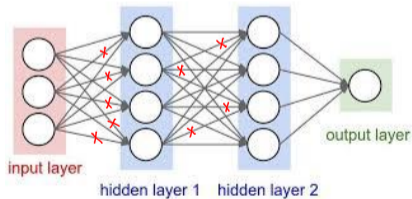


Sparsity Indicator

$\gamma_l^{(j)} = I(\theta_l^{(j)} \neq 0)$ with associated parameter vector $\theta_l^{(j)}$

Prior Distribution

$$\begin{aligned}\theta_l^{(j)} | \gamma_l^{(j)} &\sim \gamma_l^{(j)} \pi_1(\cdot; \sigma_j) + (1 - \gamma_l^{(j)}) \pi_0(\cdot; \alpha_j \sigma_j) \\ \gamma_l^{(j)} &\sim \text{Bernoulli}(\lambda)\end{aligned}$$



Key Idea

- Instance-dependent transition models can be learned by leveraging anchor points.

Detail

- \mathbf{x} is an anchor point of class k if

$$\mathbb{P}(y = k|\mathbf{x}) = 1$$

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- anchor points and their noisy labels:

$$\begin{aligned} \overline{\mathcal{D}}_0 &: \cup_{k,i} \{ \{ \mathbf{x}_i, \tilde{\mathbf{y}}_i \} : \mathbb{P}(y_i = k | \mathbf{x}_i) = 1 \} \\ n &: \text{size of } \overline{\mathcal{D}}_0 \end{aligned}$$

Learning Transition Model Algorithm

- use majority voting to determine anchor points (Li et al. 2021; Liu & Tao 2016; He, Yi & Hu 2026)
- obtain estimates of the network parameters:

$$\hat{\theta} = \arg \max_{\theta} \left\{ \sum_{i=1}^n \log p_{\theta,i} + \log \pi(\theta) \right\}$$

- determine the sparse network \implies resulting estimate for $\mathbb{P}(\tilde{y}^{(r)} | y = k, \mathbf{x})$: $f_{\theta}^{(k,r)}$

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Posterior Probability Measure

$$\Pi(G|\overline{\mathcal{D}}_0) = \frac{\int_G p_{\theta}^n(\overline{\mathcal{D}}_0) d\Pi(\theta)}{\int_{\Theta} p_{\theta}^n(\overline{\mathcal{D}}_0) d\Pi(\theta)}$$

where

- p_{θ}^n : probability density/mass function for $\overline{\mathcal{D}}_0$
- $\Pi(\cdot)$: prior for θ

Theorem 1

Let $d(\cdot, \cdot)$ denote the [Hellinger distance](#). Under regularity conditions, there exists a sequence of constants $\{\epsilon_n^2\}_{n=1}^\infty$ satisfying

$$\lim_{n \rightarrow \infty} \epsilon_n = 0 \text{ and } \lim_{n \rightarrow \infty} n\epsilon_n^2 = \infty$$

such that for $k \in [K]$ and $r \in [R]$, the posterior measure satisfies

$$\Pi \left\{ \theta \in \Theta : d(f_\theta^{(k,r)}, f_0^{(k,r)}) > M_n \epsilon_n \mid \overline{\mathcal{D}}_0 \right\} \rightarrow 0 \text{ in probability as any } M_n \rightarrow \infty$$

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Implications

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- Theorem 1 extends existing results from the [i.i.d. setting](#) (e.g., Wang & Rocková 2020; Sun, Song & Liang 2021; Sun, Xiong & Liang 2021) to the [i.n.i.d setting](#).

Proposed Prediction Method with Label-Noise Effects Accommodated

Prediction with Noisy Annotations

a new input \mathbf{x} receives labels $\tilde{\mathbf{y}} = (\tilde{y}^{(1)}, \dots, \tilde{y}^{(R)})^\top$ from R annotators

$$k^* = \arg \max_{k \in [K]} \mathbb{P}(y = k | \tilde{\mathbf{y}}^{(r)}, \mathbf{x})$$

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Problem Reformulation

- Step 1:

$$k^* = \arg \max_{k \in [K]} \left\{ \tilde{h}_k \prod_{r=1}^R \hat{\tau}_{k, \tilde{y}^{(r)}}^{(r)} \right\}$$

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class prior: \tilde{h}_k for class k

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- Step 2: Convert to that k^* wins every pairwise comparison for

any $k \neq k^*$

Hypothesis Testing:

$$H_k : \mathbb{P}(\tilde{y}|y = k, \mathbf{x}) \quad \text{versus} \quad H_{k'} : \mathbb{P}(\tilde{y}|y = k', \mathbf{x})$$

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Pairwise Test for Label Correction

– using the Neyman-Pearson Lemma

$$\frac{\hat{h}_{i,k} \prod_{r=1}^R \prod_{l=1}^K \left\{ \tau_{i,kl}^{(r)} \right\}^{1(\tilde{y}_i^{(r)}=l)}}{\hat{h}_{i,k'} \prod_{r=1}^R \prod_{l=1}^K \left\{ \tau_{i,k'l}^{(r)} \right\}^{1(\tilde{y}_i^{(r)}=l)}} > \Omega$$

Objective

derive bounds on the Bayes risk

Notation

$\overline{\mathcal{D}} = \{\mathbf{x}_i, \bar{y}_i\}_{i=1}^{\bar{n}}$:	instances with estimated labels $\bar{\mathbf{y}} = \{\bar{y}_i\}_{i=1}^{\bar{n}}$
$\mathbf{y} = \{y_i\}_{i=1}^{\bar{n}}$:	true labels
$\hat{h}(\mathbf{y})$:	prior probability of \mathbf{y}
$\boldsymbol{\tau} \triangleq \{\boldsymbol{\tau}_i^{(r)} : r \in [R]\}_{i=1}^{\bar{n}}$:	transition matrices

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Loss Function

$$\mathcal{L}(\bar{\mathbf{y}}, \mathbf{y}) = \frac{1}{\bar{n}} \sum_{i=1}^{\bar{n}} \mathbf{1}(\bar{y}_i \neq y_i)$$

Bayes Risk

$$\mathfrak{R}_{\text{Bayes}}(\hat{h}, \mathcal{L}) = \inf_{\bar{\mathbf{y}}} \left[\sum_{\mathbf{y} \in [K]^{\bar{n}}} \hat{h}(\mathbf{y}) \mathbb{E}\{\mathcal{L}(\bar{\mathbf{y}}, \mathbf{y}) | \mathbf{y}; \boldsymbol{\tau}\} \right]$$

Theorem 2

Under regularity conditions, we have that

$$\begin{aligned} & \frac{1}{\bar{n}} \left[1 - \frac{\bar{D}_{KL}(\mathbf{h}, \boldsymbol{\tau}) + \frac{1}{\bar{n}} \log(2 - \prod_{i=1}^{\bar{n}} \max_{k \in [K]} \hat{h}_{i,k})}{\{\sum_{i=1}^{\bar{n}} \log(\max_{k \in [K]} \hat{h}_{i,k})\} / \bar{n}} \right] \\ & \leq \mathfrak{R}_{\text{Bayes}}(\mathbf{h}, \mathcal{L}) \\ & \leq \frac{K-1}{\bar{n}} \sum_{i=1}^{\bar{n}} \sum_{k=1}^K \hat{h}_{i,k} \exp \left\{ -RI_{\Omega}^{(k)}(\mathbf{h}_i, \boldsymbol{\tau}_i) \right\} \end{aligned}$$

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Remarks

- Theorem 2 establishes bounds on the Bayes risk for arbitrary priors.
- The involvement of $I_{\Omega}^{(k)}(\mathbf{h}_i, \boldsymbol{\tau}_i)$ reflects how the identified upper bound of the Bayes risk may be influenced by the prior \mathbf{h}_i and the ability of annotators to distinguish between labels.

Numerical Studies

Image Datasets

- two datasets with **human annotations**:
 - **CIFAR-10N**: three independent human annotated noisy labels
 - **LabelMe**: 10,000 training images, 500 validation images, and 1,188 test images

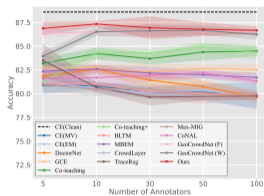
Image Datasets

- two datasets with **human annotations**:
 - **CIFAR-10N**: three independent human annotated noisy labels
 - **LabelMe**: 10,000 training images, 500 validation images, and 1,188 test images
- three datasets with **synthetic annotations**:
 - **MNIST**: 10 classes of 28×28 grayscale images
 - **CIFAR10**: 10 classes of $32 \times 32 \times 3$ color images
 - **CIFAR100**: 100 fine-grained classes of $32 \times 32 \times 3$ images
 - consider three groups of annotators with varying expertise
 - an average labeling error rate of about 20%, 35% and 50%

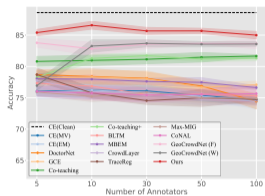
Competing Methods

- (1). **CE (Clean)**: train the network with the standard cross entropy loss on the clean datasets
- (2). **CE (MV)**: train the network using the labels from majority voting
- (3). **CE (EM)**: Dawid and Skene (1979)
- (4). **DoctorNet**: Guan, Gulshan, Dai, and (Hinton 2018)
- (5). **GCE**: Zhang and Sabuncu (2018)
- (6). **Co-teaching**: Han, Yao, Yu, Niu, Xu, Hu, Tsang, and Sugiyama (2018)
- (7). **Co-teaching+**: Yu, Han, Yao, Niu, Tsang, and Sugiyama (2019)
- (8). **BLTM**: Yang, Yang, Han, Liu, Xu, Niu, and Liu (2022)
- (9). **MBEM**: Khetan, Lipton, and Anandkumar (2017)
- (10). **CrowdLayer**: Rodrigues and Pereira (2018)
- (11). **TraceReg**: Tanno, Saeedi, Sankaranarayanan, Alexander, and Silberman (2019)
- (12). **Max-MIG**: Cao, Xu, Kong, and Wang (2019)
- (13). **CoNAL**: Chu, Ma, and Wang (2021)
- (14). **GeoCrowdNet(F)**: Ibrahim, Nguyen, and Fu (2023)
- (15). **GeoCrowdNet (W)**: Ibrahim, Nguyen, and Fu (2023)

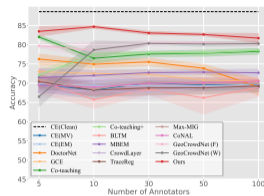
Empirical Results on CIFAR10



(a) IDN-LOW

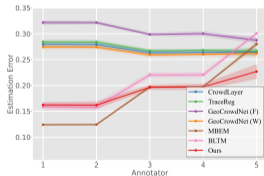


(b) IDN-MID

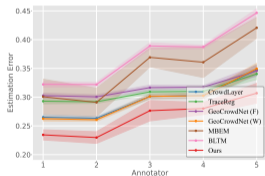


(c) IDN-HIGH

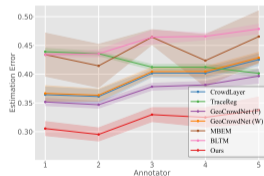
Average Accuracy



(d) IDN-LOW



(e) IDN-MID



(f) IDN-HIGH

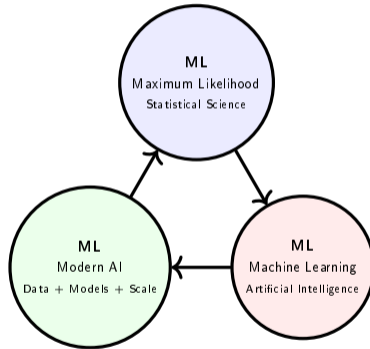
Average Estimation Error for Transition Matrices

With varying number of annotators, the proposed method

- achieves the highest average test accuracy
- leads to smallest estimation error in most of the cases, especially when the noise rate is high.

Part 4: From ML to ML

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Statistics provides principles for ML; ML generates new statistical challenges

From ML to ML:

Examples of “Invisible Victory” of Statistical Thinking



Brief Timeline of Machine Learning

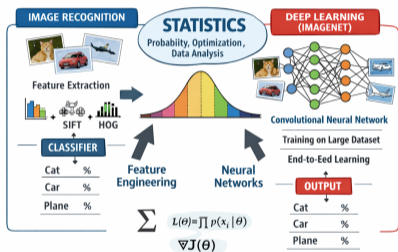


Success Stories: Statistics in Deep Learning

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Image Recognition (AlexNet)

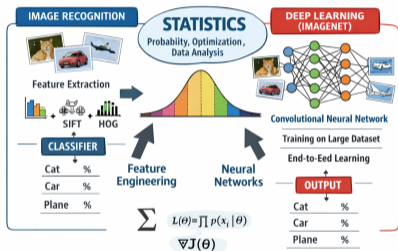
- Large-scale supervised learning (ImageNet)
+ CNNs



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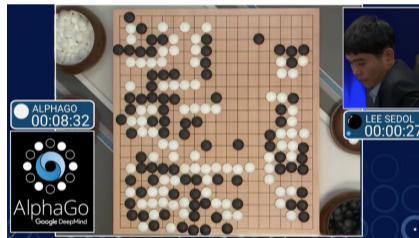
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Computer Go (AlphaGo)

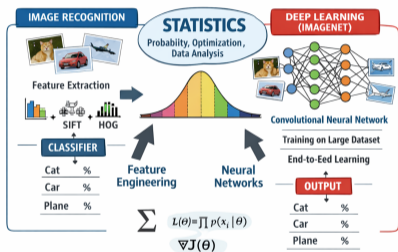
- Deep policy/value networks
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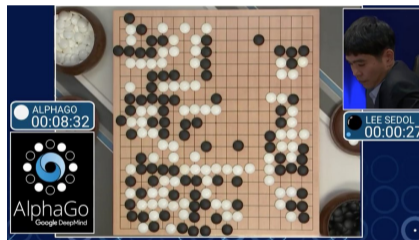


Where Statistics Is Critical

- Probabilistic modeling
- Loss & likelihood

Computer Go (AlphaGo)

- Deep policy/value networks
+ Monte Carlo Tree Search



- Monte Carlo estimation
- Stochastic approximation

Success Story: Statistics in NLP and Language Models

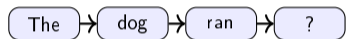
NLP → Statistical Problems:

modeling the joint distribution of word sequences via conditional probabilities

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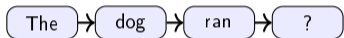


predict the next word

Success Story: Statistics in NLP and Language Models

NLP → Statistical Problems:

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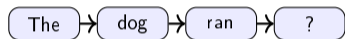
- Statistical Target:

$$P(\text{next word} \mid \text{context})$$

Success Story: Statistics in NLP and Language Models

NLP → Statistical Problems:

modeling the joint distribution of word sequences via conditional probabilities



predict the next word

- **Statistical Target:**

$$P(\text{next word} \mid \text{context})$$

- **Estimation:**

learn this conditional distribution from data

- **Inference:**

choose likely words, sentences, or translations

Raw Text Is Not Directly Usable

“The dog ran away”

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“The dog ran away”

Tokenization

[The, dog, ran, away]

Tokens = words / subwords / characters

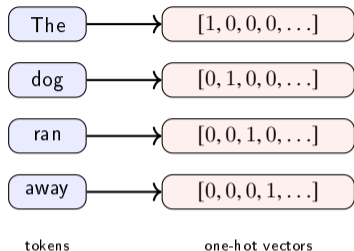
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Tokens \Rightarrow discrete random variables

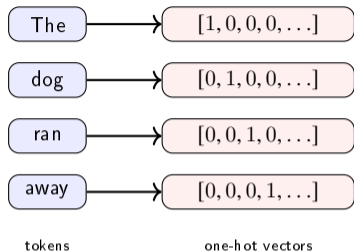
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Tokens \Rightarrow discrete random variables

- Modern ML/NLP starts with
text \rightarrow tokens \rightarrow vectors \rightarrow statistics

- Numerical representation enables statistical modeling.

Statistics in NLP: From Words to Probabilities

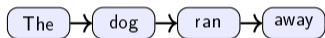
n-gram Models: Model Natural Language as Sequences

$$P(x_1, \dots, x_T) = \prod_{t=1}^T P(x_t \mid x_1, \dots, x_{t-1})$$

Statistics in NLP: From Words to Probabilities

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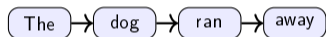
next-word prediction

- **MLE**: estimate word probabilities
- **Smoothing**: avoid zero probabilities
- **Embeddings**: reduce sparsity

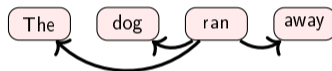
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next-word prediction



transformer attention

- **MLE**: estimate word probabilities
- **Smoothing**: avoid zero probabilities
- **Embeddings**: reduce sparsity
- **Attention Weights**: data-dependent probabilities
- **Softmax**: probability normalization
- **Training**: likelihood/cross-entropy optimization

Transformers improve learning by attending to relevant information across words and contexts.

From ML to ML:
What Machine Learning Brings to Statistics?

Perspective 1: Reliability and Risk – An Analogy with Drug Development and LLMs

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Managing Risk and Side Effects in Drug Development

- Drugs undergo **rigorous testing** before deployment.
- Risks and **side effects** are explicitly documented.
- Continuously **monitor** after deployment.
- Severe issues may lead to **recall**.

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LLMs Also Have “Side Effects”

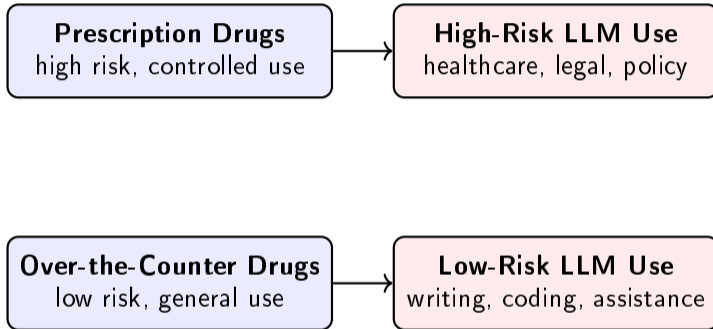
- hallucination/fabricated content:
incorrect or nonexistent facts
- data quality dependence:
noise/misinformation/outdated knowledge
- bias and fairness issues:
social/demographic/cultural bias
- safety and misuse risks:
misleading/harmful/manipulative content
- strong at correlation but weak at causal reasoning
- sensitive to prompts
- lack of reliability/calibration:
no intrinsic notion of “I don’t know”

Not All LLM Usage Should Be Treated Equally

Prescription Drugs
high risk, controlled use

Over-the-Counter Drugs
low risk, general use

Not All LLM Usage Should Be Treated Equally



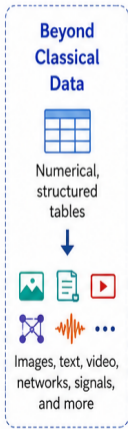
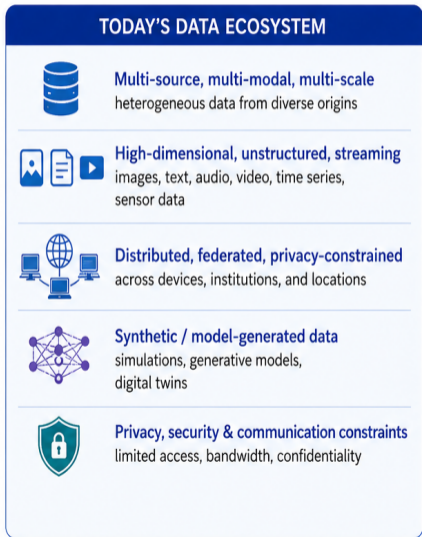
Not All LLM Usage Should Be Treated Equally



Statistical Education and Research Enables Safe and Responsible Use of AI

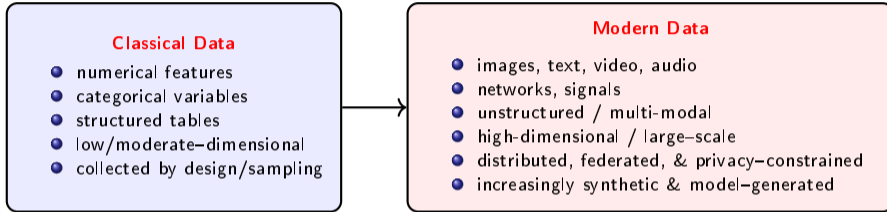
- quantify uncertainty and risk
- provide transparent “usage warnings”

Perspective 2: The Changing Nature of Data

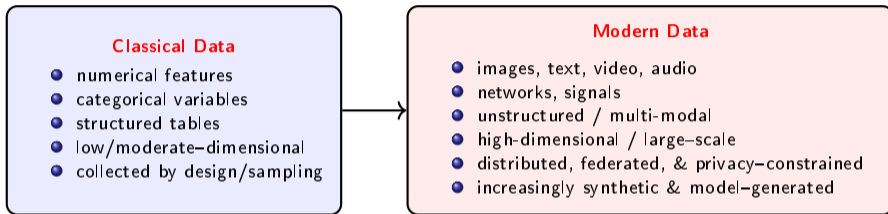


Beyond Classical Datasets, Data Today Are Richer in Nature

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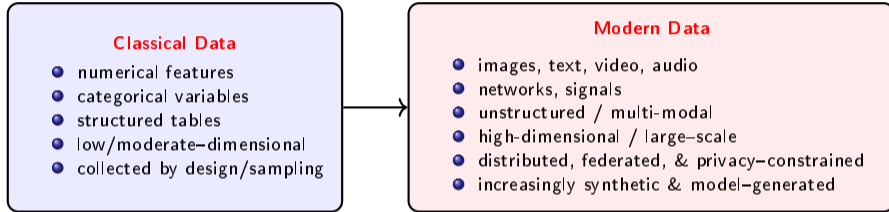
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Remarks

- more data \neq better inference
- What we can learn depends on **how we represent data**.
- Data are **no longer static** objects:
 - dynamic, streaming, and evolving

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Statistical Implications

- quality of data:
 - collection, preprocess, representation
- rethink modeling assumptions
- integrate statistics + ML
- unify theory, methods, scalable computation

Perspective 3: The Changing Nature of Modeling



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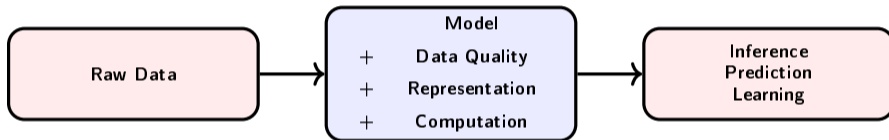
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Today, Both Fields Increasingly Share Tools and Goals

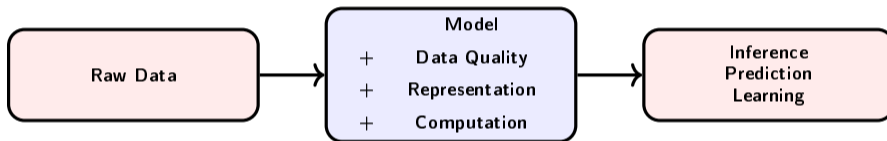
- Machine Learning: growing focus on **interpretable machine learning**.
- Statistical Science: addressing **data complexity and imperfections** with stronger **computational emphasis**.

TAKE-HOME MESSAGES



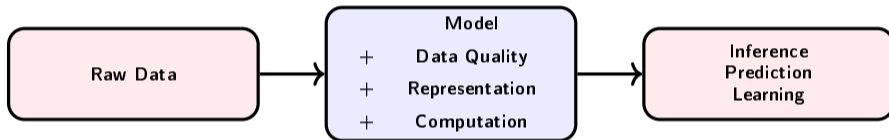
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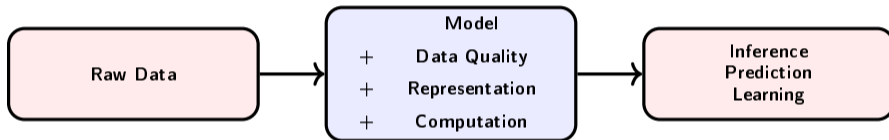
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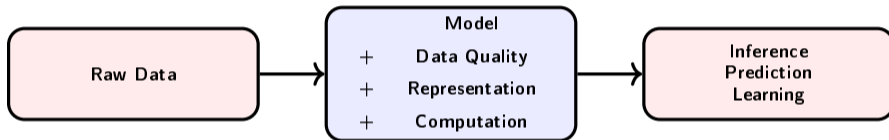


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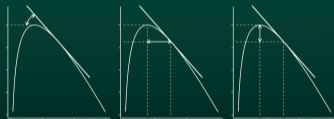


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“All data are imperfect, but some are useful – if properly represented.”
— Grace Y. Yi

Monographs on Statistics and Applied Probability 180

Likelihood and its Extensions



Nancy Reid
Cristiano Varin
Grace Y. Yi

A Chapman & Hall Book

 CRC Press
Taylor & Francis Group





Acknowledgements

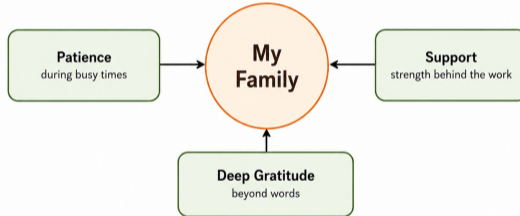


Thanks to all my collaborators and students



Thanks to My Family

*Your love, patience, encouragement, and support
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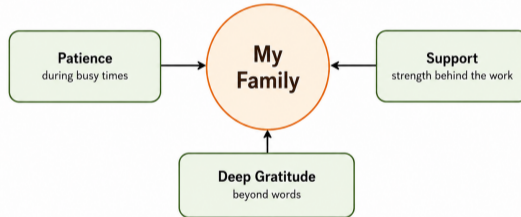
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